



# A Cellular Automata Model For Dynamics and Control of Cardiac Arrhythmias

DANNY GALLENBERGER (CARROLL UNIVERSITY)  
XIAOPENG ZHAO (UTK)  
KWAI WONG (UTK)



# Introduction

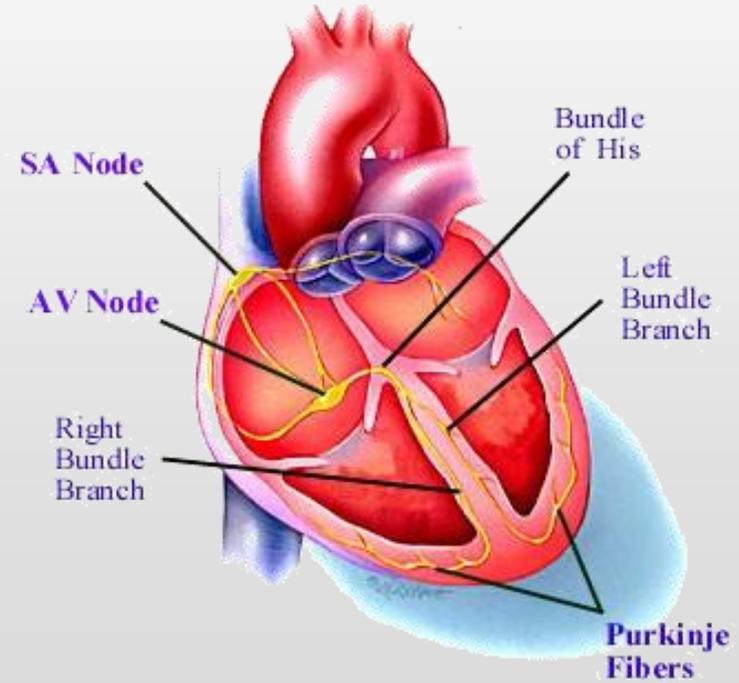
- Sudden cardiac arrest is responsible for 325,000 deaths in the US each year
- Arrhythmias
  - Not being identified in time
  - Their onset is difficult to predict
- Illustration of wave propagation through cellular automata models
  - Two-variable PDEs are computationally expensive and properties are difficult to adjust
- Control mechanisms
  - Feedback control – only effective for smaller tissue
  - Constant DI?

# Introduction

- In this study, we will look at:
  - The electrophysiological properties of the heart
  - Cardiac arrhythmias
  - How a cellular automata model can be used to analyze various scenarios
  - The functions used to simulate heart activity
  - Constant DI control through the use of electrocardiogram (ECG) data

# Electrophysiology of the Heart

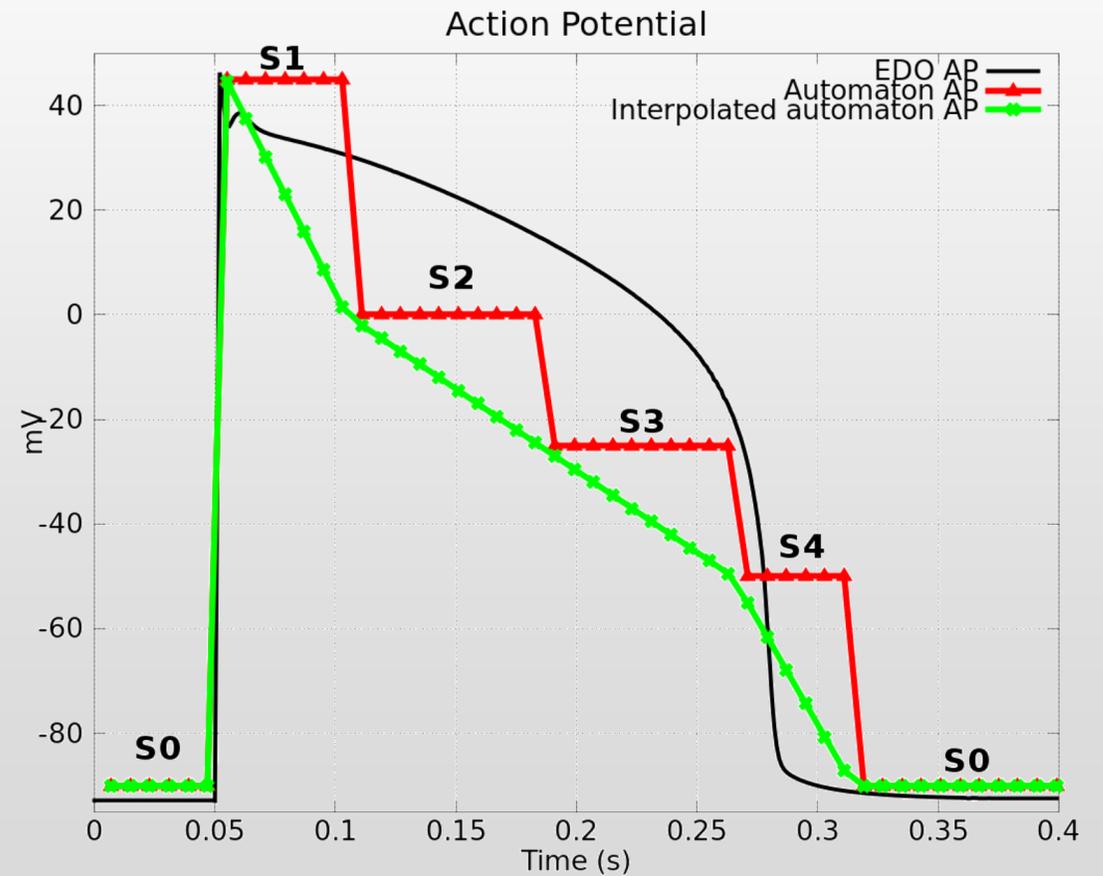
- Four chambers
- Electrical signal propagates through chambers
  - Originates in the sinus node
- As signal passes through each chamber, the heart contracts



# Electrophysiology of the Heart

## Four states

- S0 = Resting
- S1 & S2 = Excited
- S3 = Absolute Refractory
- S4 = Relative Refractory

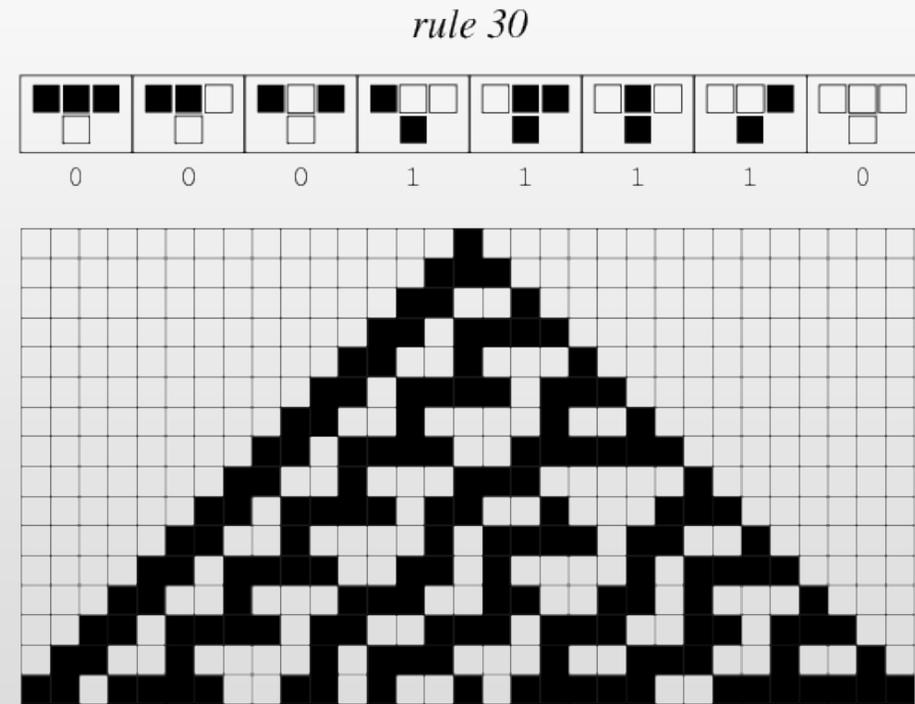


# Cardiac Arrhythmias

- A disruption in the heart's normal rhythm
- Variable Heart Rate
  - Bradycardia
  - Tachycardia
- Reentrant Arrhythmias – tissue is excited repetitively by free waves
  - Atrial Fibrillation
  - Ventricular Fibrillation
- Non-reentrant Arrhythmias
  - Alternans
  - AV Heart Block

# Cellular Automata

- Two-dimensional grid of cells
- Each cell has multiple possible states
- Predefined rules based on neighbor states
- Effective for modeling complex systems consisting of simple units
- Faster than solving PDEs



# Methods

## Steps taken:

- Analyze Mathematica simulations that run many heart scenarios
- Recreate simulation in MATLAB
- Generate action potential graphs and cellular automata models
- Generate action potential duration and ECG data
- Implement constant DI control on scenarios

# Methods

- Two-dimensional cellular automata model
- Each square represents a heart cell
- Excitation threshold = 0.9 V
- Refractory threshold = 0.1 V
- Action potential (V) of a heart cell:
  - (0.9, 1] = excited phase
  - (0.1, 0.9] = absolute refractory phase
  - (0, 0.1] = relative refractory phase
  - 0 = resting phase
- Action potential duration (APD) = time spent in excited and absolute refractory phases
- Diastolic interval (DI) = time spend in relative refractory and resting phases

# MATLAB Functions & Scripts

- **Simulation**
  - Stimulation
  - Propagation
  - Depolarization
  - Evolution
- **Parameters**
- **Restitution**
- **Action Potential**
- **Action Potential Plots**
- **Cellular Automata**
- **ECG Plots**
- $\Phi_e$  (Transmembrane Potential)

# Scenarios

## Normal Conduction

- 50x50 model
- Basic cycle length (BCL) = 75ms
- Time = 2000ms

## Normal Conduction with Scar

- 50x50 model
- Basic cycle length (BCL) = 75ms
- Time = 2000ms
- Scar cells at  $x \in [10,15]$  and  $y \in [15,20]$ 
  - Excluding (10,15), (10,20), (15,15), and (15,20)

## Spiral Wave with Scar

- 50x50 model
- Basic cycle length (BCL) = 75ms
- Time = 2000ms
- Scar cells at  $x \in [10,15]$  and  $y \in [5,10]$ 
  - Excluding (10,5), (10,10), (15,5), and (15,10)

## Alternans

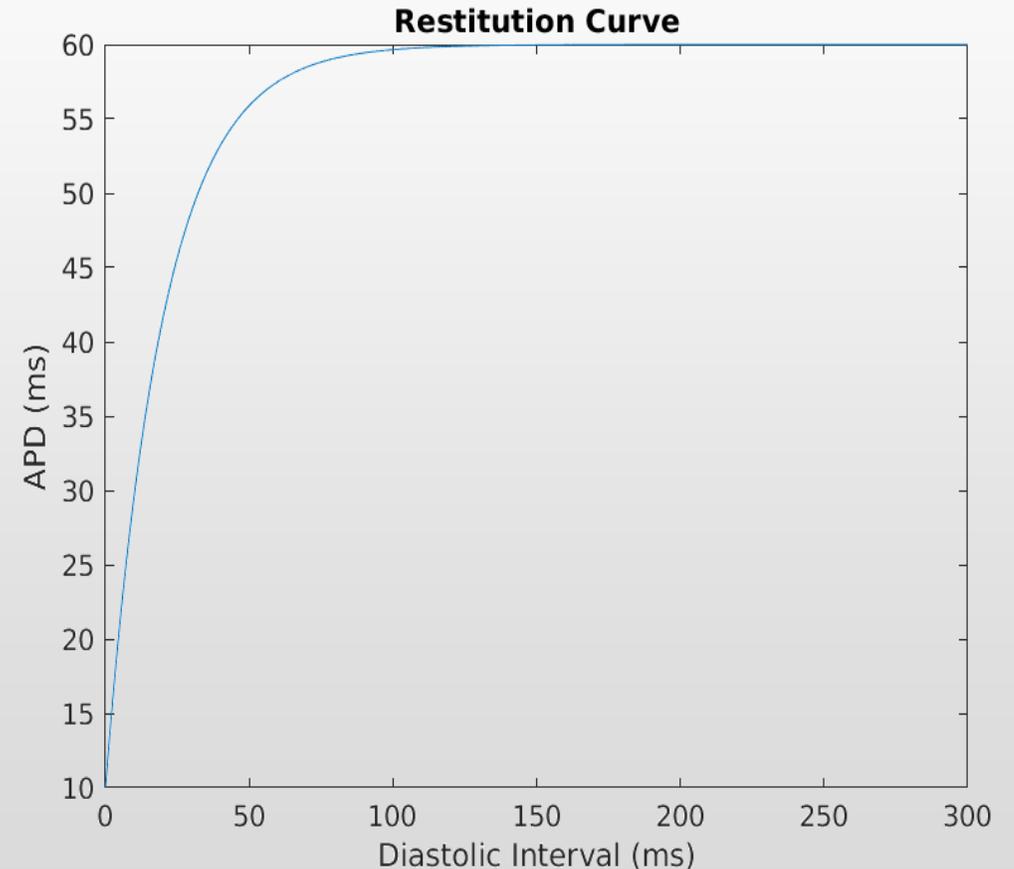
- 25x25 model
- Basic cycle length (BCL) = 54ms
- Time = 2000ms

# Other Variables

- **Stimulation Times**
  - Array of t-values at which the pacemaker cells stimulate
- **Voltage(x,y,t)**
  - Action potential of a heart cell at a given time
- **APD(x,y)**
  - Action potential duration of a heart cell
- **DI(x,y)**
  - Diastolic interval of a heart cell
- **Duration(x,y)**
  - Time elapsed since the cell's last excitation

# Restitution

- Defines the relationship between the DI and the APD
- $APD_n = f(D_{n-1})$
- $f(D_n) = A_{max} - A_0 e^{-D_n/\tau}$
- $f(D_n) = 60 - 50e^{-D_n/20}$
- As  $D_n \rightarrow \infty$ ,  $f(D_n) \rightarrow A_{max}$
- Cardiac dynamics unstable for  $f'(D_n) > |1|$



# Action Potential

- Signifies what happens to a cell after it has been stimulated as time progresses

- $f(A, t) = \frac{e^{-t/T(A)}}{c + e^{-t/T(A)}}$

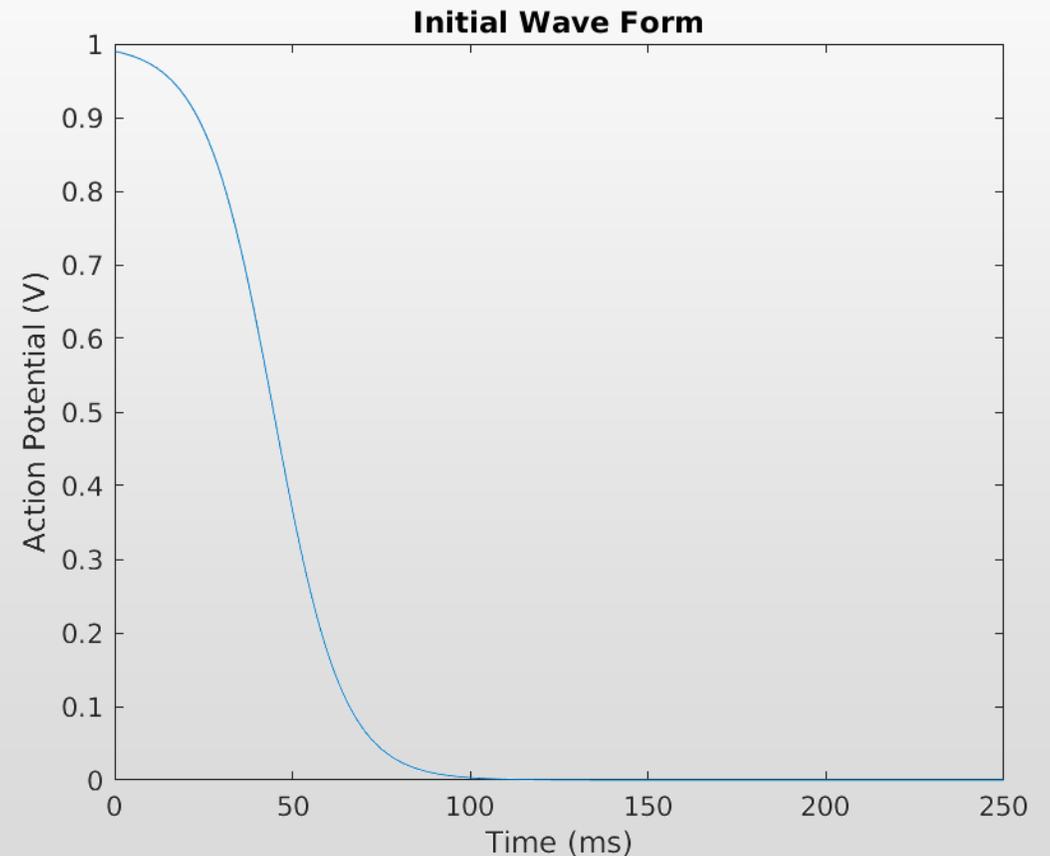
- $T(A) = \frac{A}{\ln(0.9) - \ln(0.1 * c)}$

- As  $t \rightarrow \infty$ ,  $f(A, t) \rightarrow 0$

- The greater  $A$  is, the slower the cell depolarizes

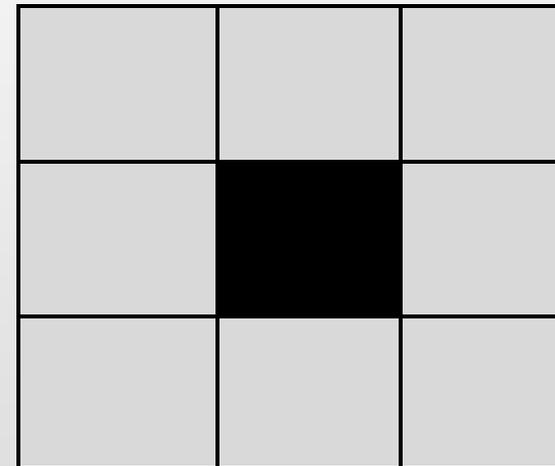
- $f(t) = \frac{e^{-t/9.7025}}{0.01 + e^{-t/9.7025}}$

- $T(66) \approx 9.7025$



# Stimulation & Wave Propagation

- **Stimulation**
  - If voltage  $\leq 0.1$ , the cell depolarizes (voltage becomes 1 V)
- **Wave Propagation**
  - If voltage  $\leq 0.1$ , the cell's neighbors are checked
  - If at least 3 neighbors are excited, the evaluated cell becomes excited
  - Otherwise, the cell evolves
- **Depolarization**
  - DI of previous heartbeat is calculated
  - APD of next beat is determined
  - Voltage becomes 1 V
  - Duration resets
- **Evolution**
  - Duration increments
  - Voltage changes based on APD and duration



Black cell is being evaluated  
Gray cells are the neighbors being checked

# Simulation

- 3x3 group of pacemaker cells stimulate at  $t = 0$
- At every time step, the propagation function is called at each cell
- If scar cells exist, they are set to 0 V
- When  $t$  reaches a stimulation time, the pacemaker cells become excited
- Process repeats until the entire interval is covered

# Constant DI

- Used as a control mechanism
- Heartbeats are regulated by DI rather than BCL
- Stimulation times are not necessarily equally spaced throughout

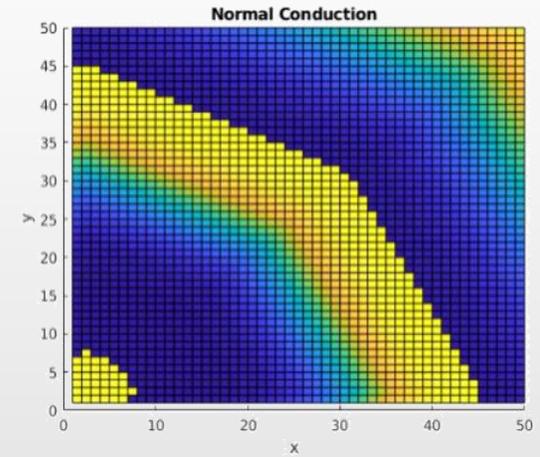
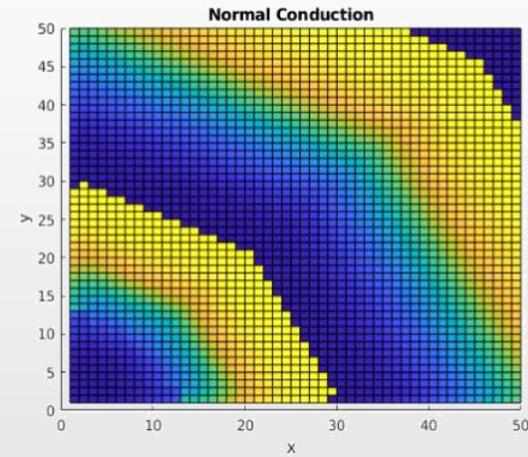
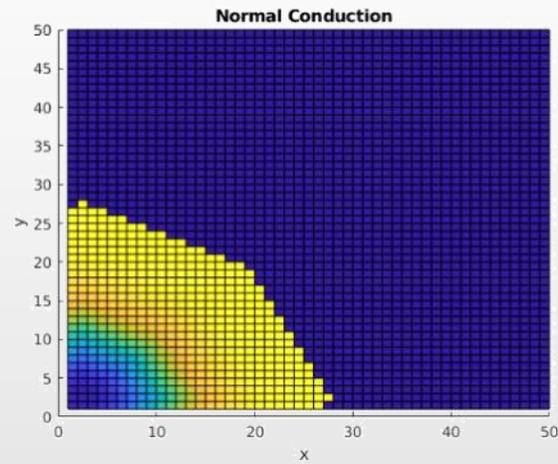
# Electrocardiogram (ECG)

- Diagram used to illustrate electrical activity in the heart
- Measures voltage difference between two points outside the tissue
- $ECG = \Phi_e(B) - \Phi_e(A)$
- $\Phi_e(x', y') = \int (-\nabla V_m) \cdot \left(\nabla \frac{1}{r}\right) dx dy$
- $r = [(x - x')^2 + (y - y')^2]^{1/2}$

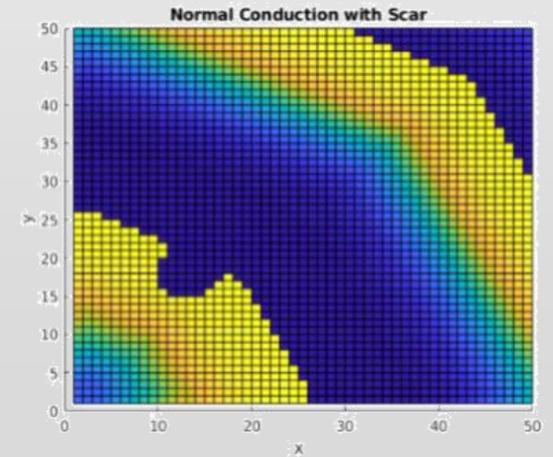
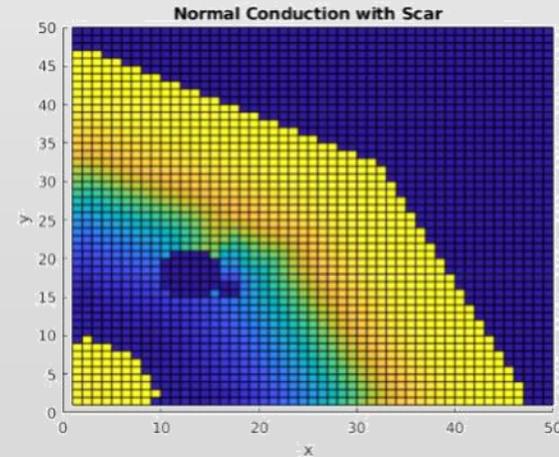
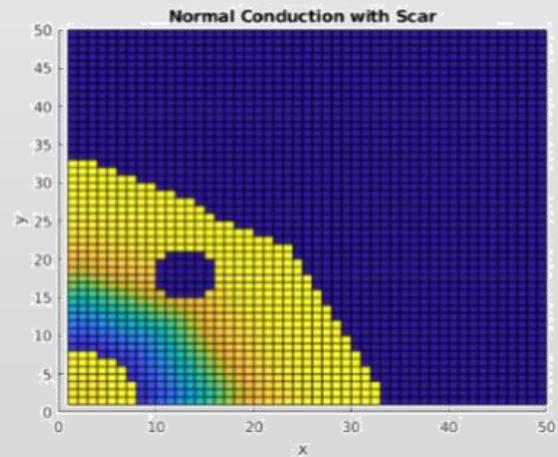


# Results

- Normal Conduction

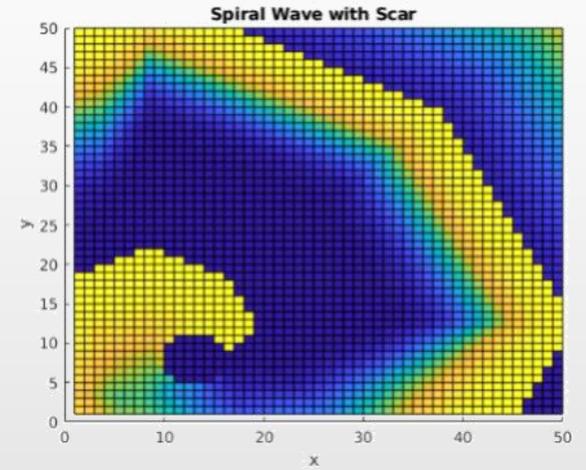
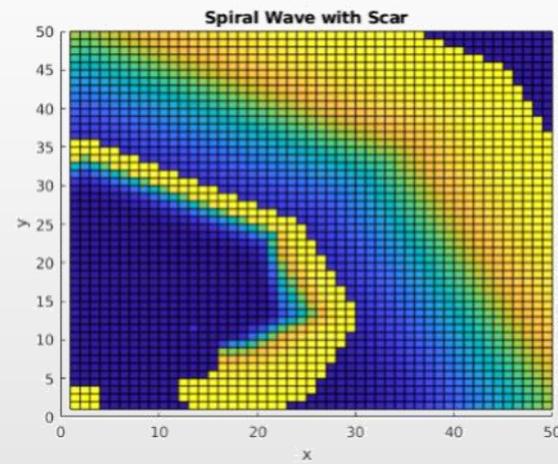
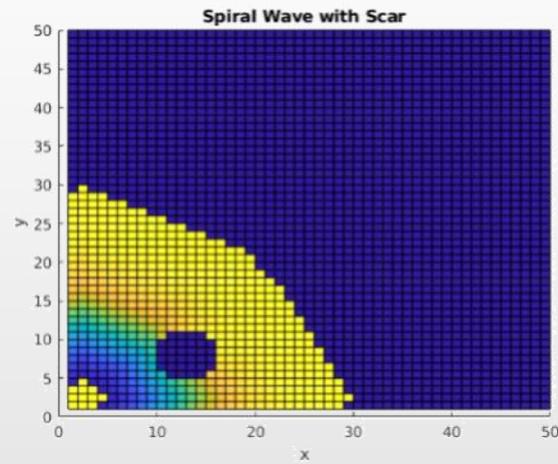


- Normal Conduction with Scar

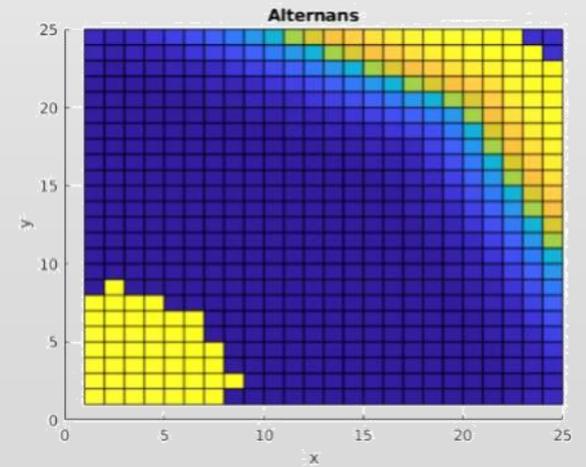
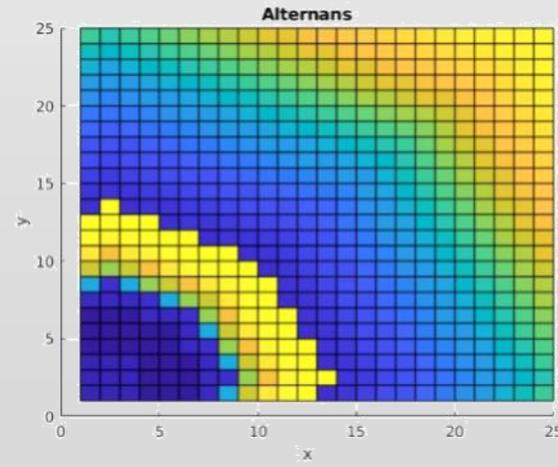
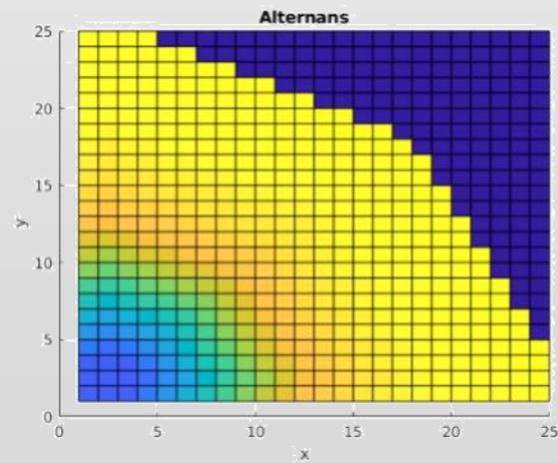


# Results

- Spiral Wave with Scar

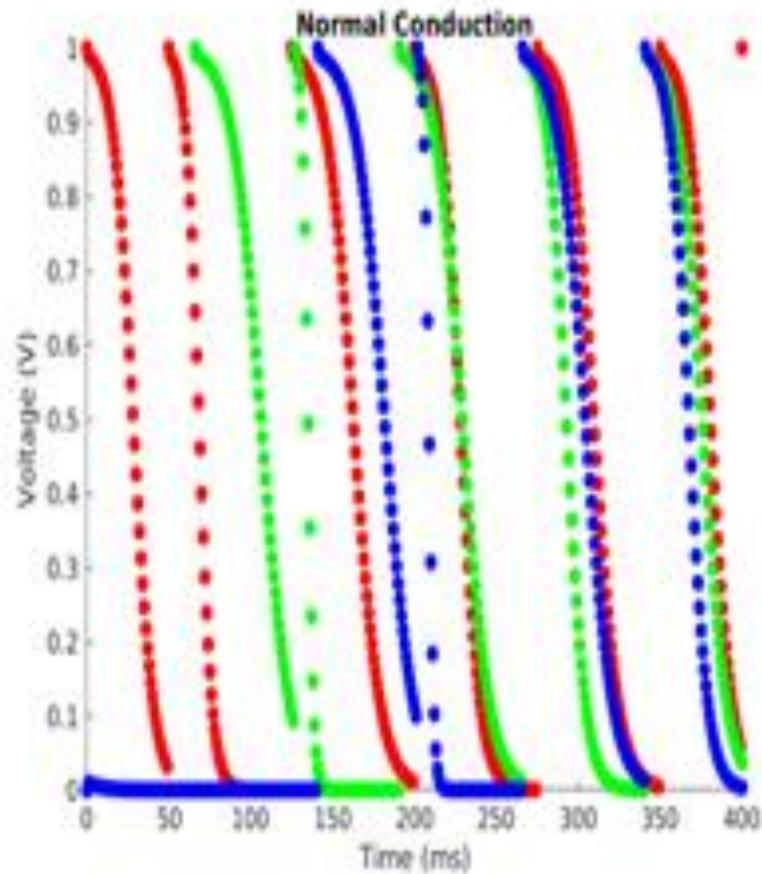


- Alternans



# Normal Conduction

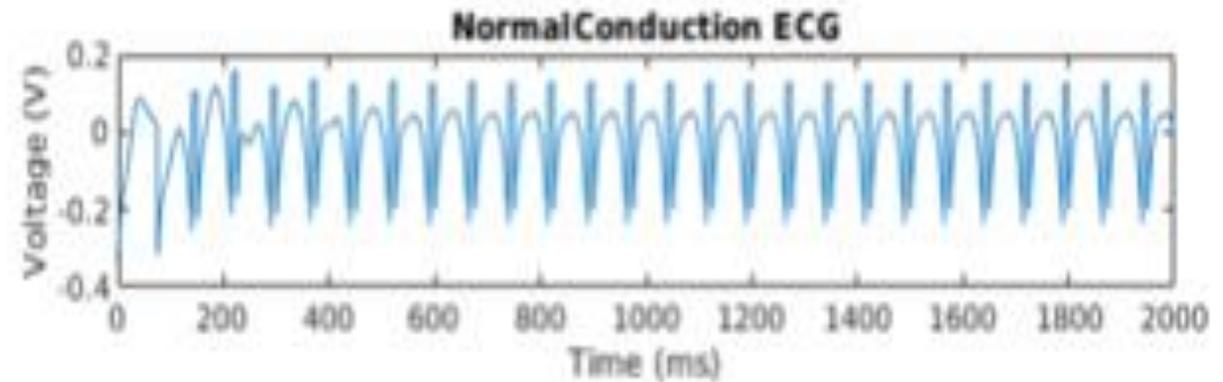
Single Cell



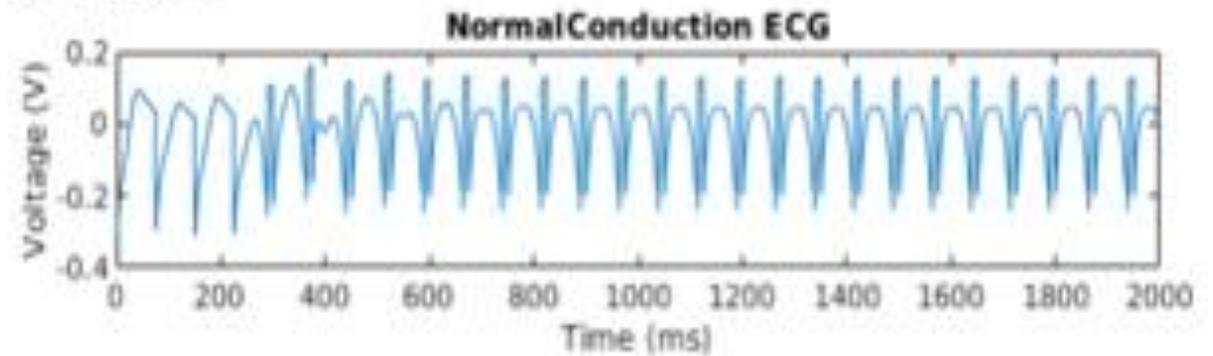
Normal  
Conduction

Tissue

50x50



100x100



# No Control vs Constant DI Control

- **No Control**

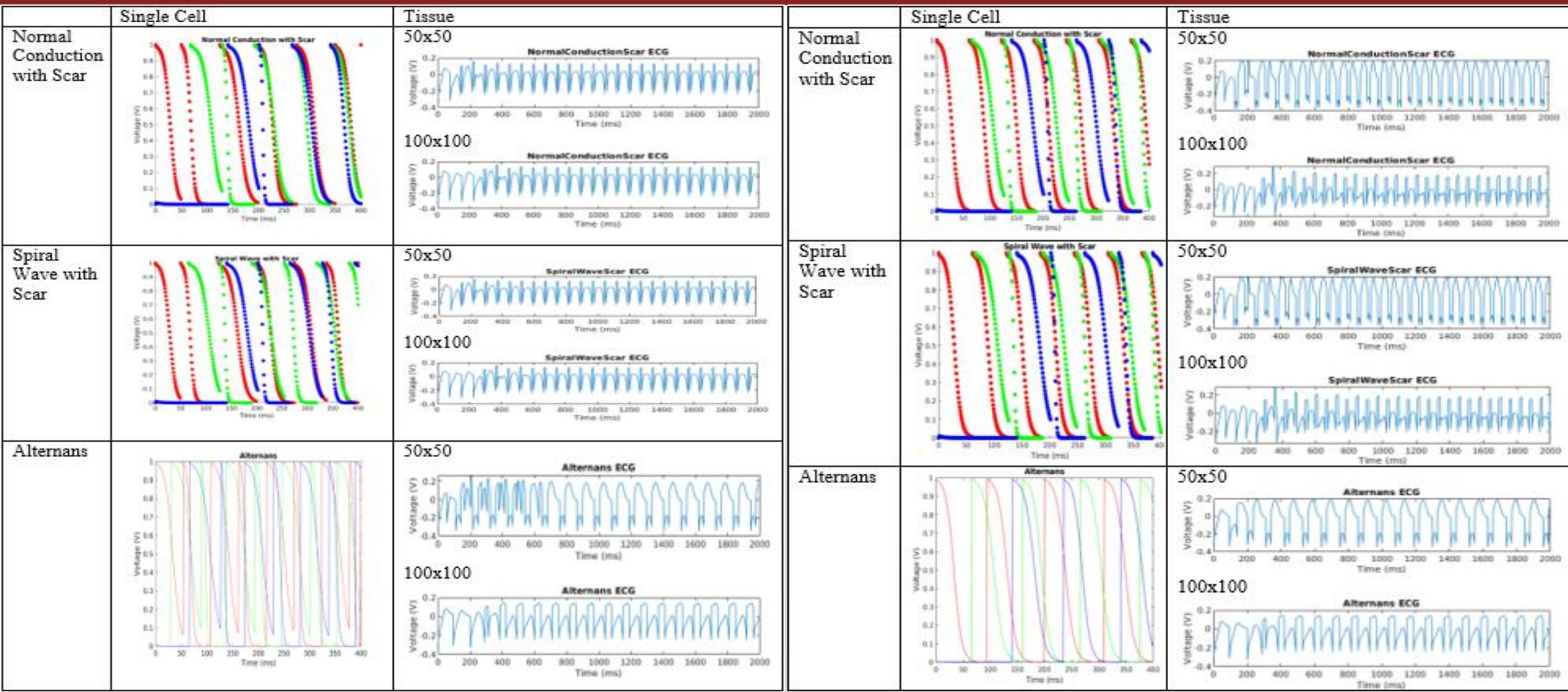
- $t_{start} = t$
- $t_{end} = t_{start} + BCL$

- **Constant DI**

- $t_{start} = t$
- $t_{end} = t_{start} + APD(1,1) + DI_{target}$

- $DI_{target} = BCL - APD(1,1)$
- $APD(1,1) = 56.5466ms$
- Normal Conduction with Scar & Spiral Wave with Scar
  - $BCL = 75ms$
  - $DI_{target} \approx 19$
- Alternans
  - $BCL = 54ms$
  - $DI_{target} \approx -2$

# No Control vs Constant DI Control



# Conclusion

- Constant DI effectively controlled alternans in smaller tissue
- Benefits of cellular automata
- Future work
  - 3D simulation
  - GPU implementation
  - Controlling other heart scenarios
  - Constant RT control
  - Other control mechanisms?

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